

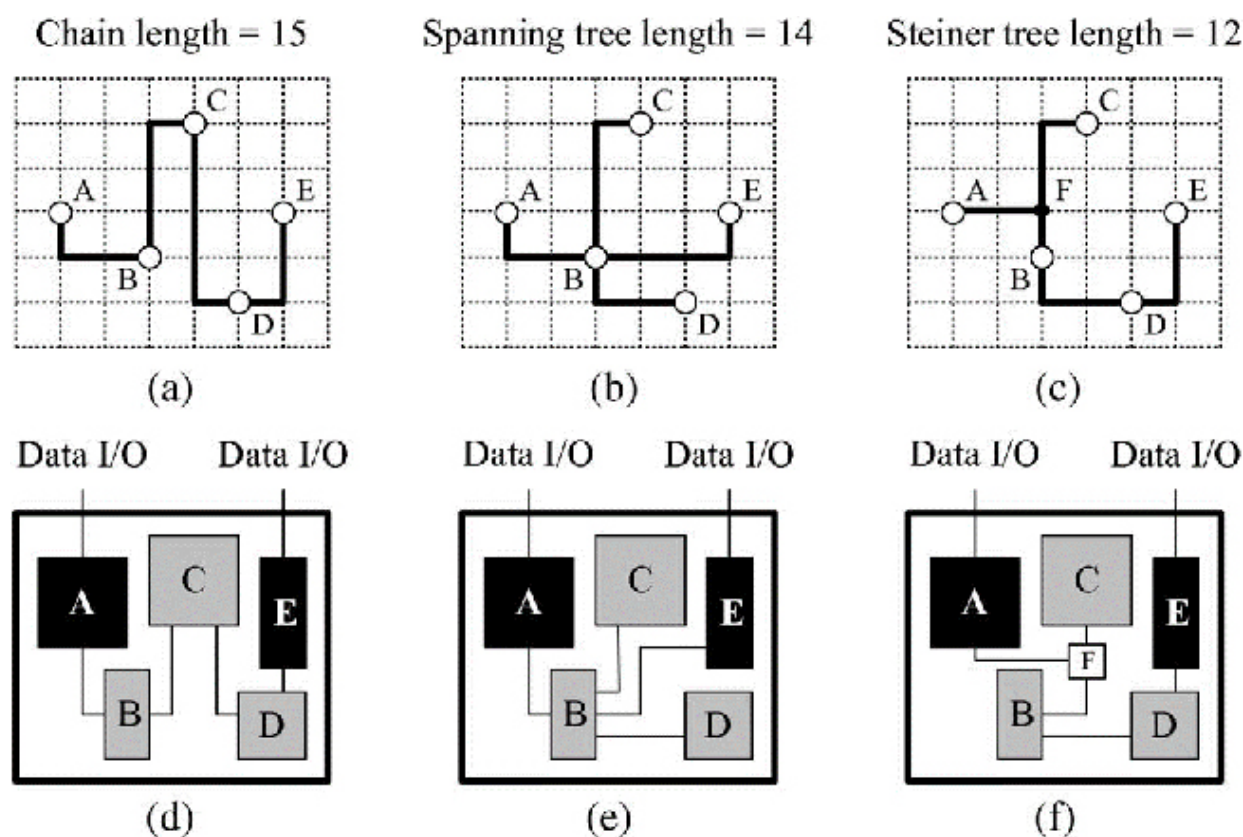
# An improved approximation ratio to the partial-terminal Steiner tree problem

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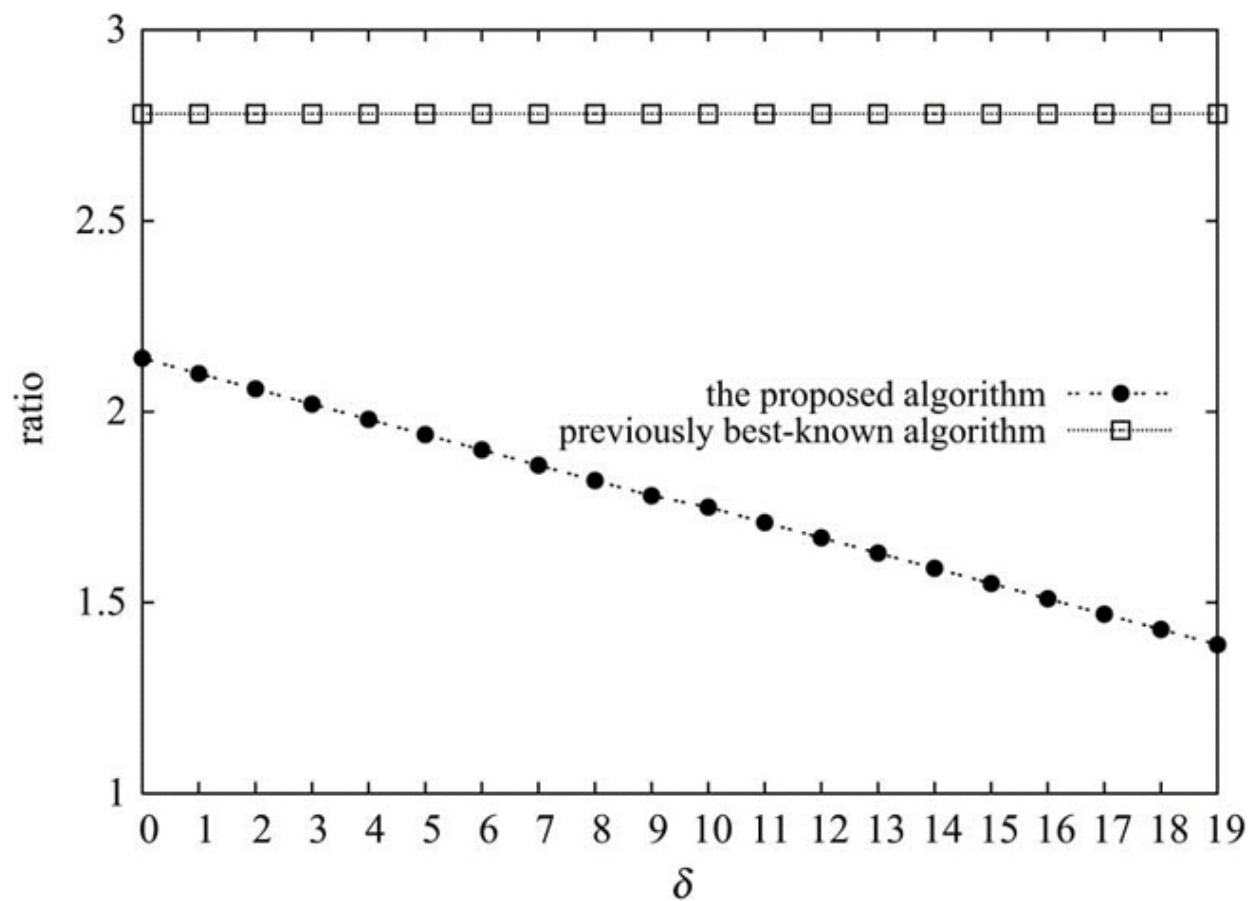
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Given a complete graph  $G = (V, E)$  with a metric cost function  $c: E \rightarrow +$  and two proper subsets  $R \subseteq V$  and  $R' \subseteq R$ , a Steiner tree is a connected and acyclic subgraph of  $G$  which contains all vertices in  $R$ . We consider a generalization of the classic Steiner tree problem and the terminal Steiner tree problem, a partial-terminal Steiner tree is a Steiner tree which contains all vertices in  $R$  such that all vertices in  $R'$  must be leaves. The partial-terminal Steiner tree problem is to find a partial-terminal Steiner tree of the minimum cost in  $G$ .



The application of the partial-terminal Steiner tree problem on IC design.

The previously best-known approximation ratio of the problem is  $2\rho$ , where  $\rho$  is the approximation ratio of the Steiner tree problem. In this paper, we improve the approximation ratio from  $2\rho$  to  $2\rho - \lfloor (\rho)/(3\rho - 2) \rfloor - f$ , where  $f$  is a non-negative function whose value is between  $0$  and  $\rho - \lfloor (\rho)/(3\rho - 2) \rfloor$ .



The approximation ratios of the proposed algorithm and previously best-known algorithm.

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